

MTH 4301: Modern Abstract Algebra

Sul Ross State University

Spring 2024

Professor: April Maria Ortiz, Ph.D.

What to Call Me: she / her / ma'am / Professor / Mrs. Ortiz / Dr. Ortiz

E-mail: april.ortiz@sulross.edu

Office: Uvalde Campus A101

Office Phone: (830) 279-3048

Cell Phone: (830) 333-0164

Course Description Congruence classes, group theory and its applications to number theory and geometry, introduction to rings, integral domains, and fields.

Mathematics Program Outcomes (1) The student will be able to demonstrate content knowledge of basic mathematical principles. (2) The student will be proficient in logic, able to negate statements, provide counterexamples to false statements, and determine the validity of arguments. (3) The student will be able to communicate mathematical content clearly and with valid reasoning.

Marketable Skills (1) Logical and analytical skills. (2) Problem-solving using analytic and algebraic methods. (3) Use of technology in problem-solving and presentation. (4) Communication and pedagogical skills.

Class Meetings Tuesday and Thursday, 2:00 – 3:15

Class Location Del Rio 107; Eagle Pass B113; Uvalde B114; Alpine ACR 206; Midland College

Required Texts Hungerford, *Abstract Algebra: An Introduction*.

Office Hours Tuesday / Thursday 2:00 – 3:00 and Monday / Wednesday 10:00 – 2:00; or by appointment; or basically whenever I'm not busy

Course Policies

Attendance Policy

Attendance is mandatory. Students are expected to attend class in person in their classroom of registration unless permission is given for extenuating circumstances. You will be held responsible for all material covered in class or in the reading assignments. If you have to miss a class, it is your responsibility to obtain all notes, assignments, and announcements from someone else in the class. Make-up exams will be given only in the event of an emergency, in which case written justification and/or documentation must be provided and approved.

Communication

I will post course documents, reminders, announcements, and assignments on the Blackboard system. You will also submit homework on Blackboard. I may also occasionally send announcements via e-mail. You should make sure you know how to access and use these tools. You are welcome to e-mail, telephone, or text me. However you chose to contact me, please make sure to state your name at the beginning of any message.

You are welcome to stop by my office if you wish to speak about the content or your progress

in the course. Sometimes meetings come up, so it's best to contact me ahead of time if you intend to travel to Uvalde to see me in person.

I am here to help you! Ask questions in class, call me, e-mail me, text me, or come to my office. If you don't communicate with me, then I can't help you.

Grading Policy

Your grades will be weighted as follows:

Participation	10%
Homework	25%
Midterm Exam	25%
Final Exam	40%

A student who averages at least 90% will receive an A; at least 80% will receive at least a B; at least 70% will receive at least a C; at least 60% will receive at least a D.

Participation

Your participation grade will be assigned depending on your class attendance and participation in class activities. Simply put, if you always come to class, seem like you're trying to pay attention and take notes, and take part in class activities, then you will get full credit.

Homework

Homework is the most essential component of the course. It is important that you attempt to complete each assignment before the next class period. This will allow us to make the most of our time together. We will always have time in class to discuss homework.

Each week, you will submit exercises to be graded for correctness. Homework can be submitted in a variety of formats, but each assignment must be submitted as a single file that I can view and grade on Blackboard.

One possibility would be to type up your homework using the Equation Editor on Microsoft Word and save it as a PDF. Another would be to capture high-quality images of your homework using a phone or other device and combine into a single file, e.g. by pasting each image into a word processor file. Feedback will be provided in the form of comments your Blackboard file.

All work must be shown for full credit. Try to be as tidy as possible so that I can understand your work. I'm flexible as to file format provided I can view your submission on Blackboard. Submissions consisting of multiple image files will not be graded as it's too easy for me to lose my place and miss something. If I have trouble seeing your file, I will let you know and give you a chance to resubmit.

Exams

There will be one midterm exam. Its tentative date is Wednesday, March 6. This is subject to change. You will be notified of a change at least one week in advance. Make-up exams will be given only in the event of an emergency, in which case written justification and/or documentation must be provided and approved.

The comprehensive final exam will take place at the time scheduled by the university, during the final exam period at the end of the semester. Official time and date to be announced once the university publishes the final exam schedule.

Subject Outline

Below is a tentative outline of the subjects we will cover in this course.

I. Arithmetic in \mathbb{Z} Revisited

1. The Division Algorithm: *the Well-Ordering Axiom – the division algorithm*
2. Divisibility: *definition – the greatest common divisor – relative primality*
3. Primes and Unique Factorization: *prime integers – the Fundamental Theorem of Arithmetic – testing for primality*

II. Congruence in \mathbb{Z} and Modulus Arithmetic

1. Congruence and Congruence Classes: *congruence modulo n – congruence classes – the set \mathbb{Z}_n*
2. Modulus Arithmetic: *arithmetic in \mathbb{Z}_n*
3. The Structure of \mathbb{Z}_p and \mathbb{Z}_n : *notation – the structure of \mathbb{Z}_p where p is prime – units and zero divisors*

III. Groups

1. Definitions and Examples: *basic definition – permutation groups – dihedral groups – matrix groups*
2. Basic Properties of Groups
3. Subgroups: *definition – basic criteria – the center of a group – cyclic subgroups – group generators*
4. Isomorphisms and Homomorphisms: *isomorphisms and automorphisms – homomorphisms – Cayley's Theorem*

IV. Symmetry

1. Symmetric and Alternating Groups: *the symmetric group – cycles – transpositions – even and odd permutations – the alternating group*
2. Ornamental Symmetry: *the rotational group – subgroups – realizations – the dihedral group – direct sums and products – translations – frieze groups – wallpaper groups – polyhedral and crystal groups*

Schedule

This schedule is tentative only. The section numbers refer to the outline above.

January 17 – February 14	Unit I
February 14 – March 4	Unit II
March 6	Midterm Exam
<i>March 11 – 15</i>	<i>Spring Break</i>
March 18 – April 10	Unit III
April 10 – May 1	Unit IV
May X	Final Exam

University Statements

Distance Education Statement. *Students enrolled in distance education courses have equal access to the university's academic support services, such as library resources, online databases, and instructional technology support. For more information about accessing these resources, visit the SRSU website.*

Students should correspond using Sul Ross email accounts and submit online assignments through Blackboard, which requires a secure login. Students enrolled in distance education courses at Sul Ross are expected to adhere to all policies pertaining to academic honesty and appropriate student conduct, as described in the student handbook. Students in web-based courses must maintain appropriate equipment and software, according to the needs and requirements of the course, as outlined on the SRSU website. Directions for filing a student complaint are located in the student handbook.

SRSU Accessibility Services. *Sul Ross State University (SRSU) is committed to equal access in compliance with the Americans with Disabilities Act of 1973. It is SRSU policy to provide reasonable accommodations to students with documented disabilities. It is the student's responsibility to initiate a request each semester for each class. Students seeking accessibility/accommodations services must contact Mrs. Mary Schwartze Grisham, LPC, SRSU's Accessibility Services Director at 432-837-8203 or email mschwartz@sulross.edu. Our office is located on the first floor of Ferguson Hall, room 112, and our mailing address is P.O. Box C122, Sul Ross State University, Alpine, Texas, 79832.*

Counseling Services. *Sul Ross has partnered with TimelyCare where all SR students will have access to nine free counseling sessions. You can learn more about this 24/7/356 support by visiting [Timelycare/SRSU](https://www.timelycare.com). The SR Counseling and Accessibility Services office will continue to offer in-person counseling in Ferguson Hall room 112 (Alpine campus), and telehealth Zoom sessions for remote students and RGC students.*

Libraries. *The Bryan Wildenthal Memorial Library in Alpine offers FREE resources and services to the entire SRSU community. Access and borrow books, articles, and more by visiting the library's website, library.sulross.edu. Off-campus access requires logging in with your Lobold and password. Librarians are a tremendous resource for your coursework and can be reached in person, by email (srsulibrary@sulross.edu), or by phone (432-837-8123).*

No matter where you are based, public libraries and many academic and special libraries welcome the general public into their spaces for study. SRSU TexShare Cardholders can access additional

services and resources at various libraries across Texas. Learn more about the TexShare program by visiting library.sulross.edu/find-and-borrow/texshare or ask a librarian by emailing srsulibrary@sulross.edu.

Mike Fernandez, SRSU Librarian, is based in Eagle Pass (Building D-129) to offer specialized library services to students, faculty, and staff. Utilize free services such as InterLibrary Loan (ILL) and ScanIt to get materials delivered to you at home or via email.